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Carbon dioxide absorption into monoethanolamine in a continuous film contactor

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Abstract

Numerical approach for analyzing absorption rate and understanding of the micro level interactions of various processes going inside the reactor was proposed by developing a mathematical model. The usefulness of this approach is demonstrated by presenting the analysis of experimental data for CO_2 absorption into aqueous solutions of monoethanolamine. A continuous film contactor has been designed and developed for carrying out the absorption studies experimentally. The model equations were solved using computer code in conjunction with a non-linear regression technique to estimate a correlation, first of its kind, for physical gas-phase mass transfer coefficient. Proposed numerical scheme simulates the results based on momentum, mass and heat balance at the gas–liquid interface to explain the absorption behaviour. Results showed a good agreement between experimental and model predictions, thereby suggesting the utility of the model in predicting the chemical gas-absorption performance of gas liquid contactors.

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1. Introduction

Gas absorption using liquid absorbents is one of the common mass-transfer operations widely used in industries for separating gases that are useful, toxic or environmentally unfavourable species. Separating carbon dioxide (CO₂) from flue gases exhausted by fossil-fuel-fired power plants, pharmaceutical industry, petroleum industry, etc., a potential measure to mitigate the human-originated greenhouse effect, requires the use of a gas-liquid contact device that efficiently removes CO₂ from a flue-gas flow at an enormously high rate without imposing on the flow such a substantial pressure loss as to necessitate the addition of a flue-gas compression process. Thus for treating huge amount of low-pressure (not much higher than atmospheric pressure) gases of no further use, it is critically important to devise gas-liquid contactors that allow effective gas absorption without pressurizing the gases to balance the hydrodynamic pressure losses inside the contactors. Packed columns have been widely used in industries for separation

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and purification processes involving gas and liquid contact (such as distillation and absorption) due to its high efficiency and high capacity but are not well suited for processing huge amounts of industrial waste gases due to inevitable insufficient contact-area-to-volume ratios and large gas-side pressure losses during operation. Thus from all the available designs, continuous film contactors for processing flue gases or other industrial waste gases are considered to be more advantageous. These are vertical columns where liquid flows downward wetting the wall while the gas flow counter currently contacting the liquid.

Various technologies have been developed for CO_2 and H_2S removal from gas streams. These include absorption by chemical and physical solvents, cryogenic separation and membrane separation. Gas absorption by chemical solvents such as aqueous solution of alkanolamine is one of the most popular and effective methods compared to other methods. Absorption of gas using alkanolamines has been practiced in industry for over half a century; however, it is only recently that substantial progress has been made in developing a fundamental understanding of these seemingly simple processes. A number of mathematical models for falling film reactors have been proposed [1–8] in the field of absorption, however limited attempts have been to include

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Nomenclature

$a_{\rm c}$	correction factor for the interfacial area, $R_{\rm w}(d - 2s)/d$	
٨	20)/a	
A h	gaseous reactant	
U D	liquid reactent	
D	inquid reactant a_{22} $(1/2)^{m^3}$	
C	concentration of dissolved gas Λ (kmol/m ³)	
$C_{\rm A}$	concentration of dissolved gas A (kmol/m^2)	
C_{AG}	concentration of A in bulk gas (kmol/m^3)	
$C_{\rm B}$	concentration of reactant \mathbf{B} (kmol/m ²)	
C _B	molar heat capacity of cas (I/kmol K)	
CG	heat capacity of liquid $(1/m^3 K)$	
$c_p \rho$	inear diameter of the column (m)	
u D	diffusivity of A in liquid (m^2/s)	
$D_{\rm A}$	diffusivity of R in liquid (m^2/s)	
$D_{\rm B}$	diffusion coefficient of CO ₂ in $cos(m^2/s)$	
DG f	friction coefficient	
J F	dimensionless group containing flow rates and	
1	fluid properties defined in Eq. (15)	
a	acceleration of gravity (m/s^2)	
$\frac{\delta}{hc}$	heat transfer coefficient in gas phase (I/s $m^2 K$)	
H_{a}	Henry's constant (kmol/m ³) _{max} /(kmol/m ³) _{limit}	
$-\Delta H_{\rm P}$	heat of reaction (I/kmol)	
$-\Delta H_{\rm S}$	heat of solution (I/kmol)	
k	second order rate constant at a temperature T_r	
	$(m^3/lmolo)$	
	(III ^e /KIIIOI S)	
k _G	mass transfer coefficient (m/s)	
$k_{ m G} k_{\lambda}$	mass transfer coefficient (m/s) thermal conductivity of liquid (J/s m K)	
$k_{ m G} \ k_\lambda \ L$	mass transfer coefficient (m/s) thermal conductivity of liquid (J/s m K) height of the column (m)	
$k_{ m G} \ k_{\lambda} \ L \ Q_{ m G}$	(m ² /kmors) mass transfer coefficient (m/s) thermal conductivity of liquid (J/s m K) height of the column (m) volumetric flow rate of gas (m ³ /s)	
$k_{ m G} k_{\lambda} L Q_{ m G} r$	(m ² /kmors) mass transfer coefficient (m/s) thermal conductivity of liquid (J/s m K) height of the column (m) volumetric flow rate of gas (m ³ /s) rate of reaction (kmol/m ³ s)	
k _G k _λ L Q _G r R	(m ² /kmols) mass transfer coefficient (m/s) thermal conductivity of liquid (J/s m K) height of the column (m) volumetric flow rate of gas (m ³ /s) rate of reaction (kmol/m ³ s) gas constant (J/kmol K)	
$k_{\rm G}$ k_{λ} L $Q_{\rm G}$ r R $R_{\rm A}$	mass transfer coefficient (m/s) thermal conductivity of liquid (J/s m K) height of the column (m) volumetric flow rate of gas (m ³ /s) rate of reaction (kmol/m ³ s) gas constant (J/kmol K) rate of gas absorption (kg/s)	
$k_{\rm G}$ k_{λ} L $Q_{\rm G}$ r R $R_{\rm A}$ $Re_{\rm G}$	mass transfer coefficient (m/s) thermal conductivity of liquid (J/s m K) height of the column (m) volumetric flow rate of gas (m ³ /s) rate of reaction (kmol/m ³ s) gas constant (J/kmol K) rate of gas absorption (kg/s) gas-phase Reynolds number, $(d - 2\delta)u_G\rho_G/\mu_G$	
$k_{ m G}$ k_{λ} L $Q_{ m G}$ r R $R_{ m A}$ $Re_{ m G}$ $Re_{ m L}$	mass transfer coefficient (m/s) thermal conductivity of liquid (J/s m K) height of the column (m) volumetric flow rate of gas (m ³ /s) rate of reaction (kmol/m ³ s) gas constant (J/kmol K) rate of gas absorption (kg/s) gas-phase Reynolds number, $(d - 2\delta)u_G\rho_G/\mu_G$ liquid-phase Reynolds number, $4\Gamma/\mu_L$	
$k_{\rm G}$ k_{λ} L $Q_{\rm G}$ r R $R_{\rm A}$ $Re_{\rm G}$ $Re_{\rm L}$ $R_{\rm W}$	mass transfer coefficient (m/s) thermal conductivity of liquid (J/s m K) height of the column (m) volumetric flow rate of gas (m ³ /s) rate of reaction (kmol/m ³ s) gas constant (J/kmol K) rate of gas absorption (kg/s) gas-phase Reynolds number, $(d - 2\delta)u_G\rho_G/\mu_G$ liquid-phase Reynolds number, $4\Gamma/\mu_L$ ratio of the interfacial area in the presence of	
$k_{ m G}$ k_{λ} L $Q_{ m G}$ r R $R_{ m A}$ $Re_{ m G}$ $Re_{ m L}$ $R_{ m W}$	mass transfer coefficient (m/s) thermal conductivity of liquid (J/s m K) height of the column (m) volumetric flow rate of gas (m ³ /s) rate of reaction (kmol/m ³ s) gas constant (J/kmol K) rate of gas absorption (kg/s) gas-phase Reynolds number, $(d - 2\delta)u_G\rho_G/\mu_G$ liquid-phase Reynolds number, $4\Gamma/\mu_L$ ratio of the interfacial area in the presence of waves to the plane interfacial area	
$ \begin{array}{c} k_{\rm G} \\ k_{\lambda} \\ L \\ Q_{\rm G} \\ r \\ R \\ R_{\rm A} \\ Re_{\rm G} \\ Re_{\rm L} \\ R_{\rm W} \\ Sc_{\rm G} \end{array} $	mass transfer coefficient (m/s) thermal conductivity of liquid (J/s m K) height of the column (m) volumetric flow rate of gas (m ³ /s) rate of reaction (kmol/m ³ s) gas constant (J/kmol K) rate of gas absorption (kg/s) gas-phase Reynolds number, $(d - 2\delta)u_G\rho_G/\mu_G$ liquid-phase Reynolds number, $4\Gamma/\mu_L$ ratio of the interfacial area in the presence of waves to the plane interfacial area Schmidt number, $\mu_G/\rho_G D_G$	
$ \begin{array}{c} k_{\rm G} \\ k_{\lambda} \\ L \\ Q_{\rm G} \\ r \\ R \\ R_{\rm A} \\ Re_{\rm G} \\ Re_{\rm L} \\ R_{\rm W} \\ \\ Sc_{\rm G} \\ Sh_{\rm G} \end{array} $	mass transfer coefficient (m/s) thermal conductivity of liquid (J/s m K) height of the column (m) volumetric flow rate of gas (m ³ /s) rate of reaction (kmol/m ³ s) gas constant (J/kmol K) rate of gas absorption (kg/s) gas-phase Reynolds number, $(d - 2\delta)u_G\rho_G/\mu_G$ liquid-phase Reynolds number, $4\Gamma/\mu_L$ ratio of the interfacial area in the presence of waves to the plane interfacial area Schmidt number, $\mu_G/\rho_G D_G$ Sherwood number, k_Ga_cd/D_G	
$k_{ m G}$ k_{λ} L $Q_{ m G}$ r R $R_{ m A}$ $Re_{ m G}$ $Re_{ m L}$ $R_{ m W}$ $Sc_{ m G}$ $Sh_{ m G}$ T	mass transfer coefficient (m/s) thermal conductivity of liquid (J/s m K) height of the column (m) volumetric flow rate of gas (m ³ /s) rate of reaction (kmol/m ³ s) gas constant (J/kmol K) rate of gas absorption (kg/s) gas-phase Reynolds number, $(d - 2\delta)u_G\rho_G/\mu_G$ liquid-phase Reynolds number, $4\Gamma/\mu_L$ ratio of the interfacial area in the presence of waves to the plane interfacial area Schmidt number, $\mu_G/\rho_G D_G$ Sherwood number, $k_G a_c d/D_G$ liquid temperature (K)	
$ \begin{array}{c} k_{\rm G} \\ k_{\lambda} \\ L \\ Q_{\rm G} \\ r \\ R \\ R_{\rm A} \\ Re_{\rm G} \\ Re_{\rm L} \\ R_{\rm W} \\ \\ Sc_{\rm G} \\ Sh_{\rm G} \\ T \\ T_{\rm G} \end{array} $	mass transfer coefficient (m/s) thermal conductivity of liquid (J/s m K) height of the column (m) volumetric flow rate of gas (m ³ /s) rate of reaction (kmol/m ³ s) gas constant (J/kmol K) rate of gas absorption (kg/s) gas-phase Reynolds number, $(d - 2\delta)u_G\rho_G/\mu_G$ liquid-phase Reynolds number, $4\Gamma/\mu_L$ ratio of the interfacial area in the presence of waves to the plane interfacial area Schmidt number, $\mu_G/\rho_G D_G$ Sherwood number, $k_G a_c d/D_G$ liquid temperature (K) gas-phase temperature (K)	
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$\begin{array}{c} k_{\rm G} \\ k_{\lambda} \\ L \\ Q_{\rm G} \\ r \\ R \\ R_{\rm A} \\ Re_{\rm G} \\ Re_{\rm L} \\ R_{\rm W} \\ \\ Sc_{\rm G} \\ Sh_{\rm G} \\ T \\ T_{\rm G} \\ T_{\rm G} \\ T_{\rm R} \\ u_{\rm L} \\ u_{\rm G} \\ U \end{array}$	mass transfer coefficient (m/s) thermal conductivity of liquid (J/s m K) height of the column (m) volumetric flow rate of gas (m ³ /s) rate of reaction (kmol/m ³ s) gas constant (J/kmol K) rate of gas absorption (kg/s) gas-phase Reynolds number, $(d - 2\delta)u_G\rho_G/\mu_G$ liquid-phase Reynolds number, $4\Gamma/\mu_L$ ratio of the interfacial area in the presence of waves to the plane interfacial area Schmidt number, $\mu_G/\rho_G D_G$ Sherwood number, $k_G a_c d/D_G$ liquid temperature (K) gas-phase temperature (K) inlet liquid temperature (K) temperature of cooling water (K) axial velocity of liquid film (m/s) velocity of gas film (m/s)	
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$k_{\rm G}$ k_{λ} L $Q_{\rm G}$ r R $R_{\rm A}$ $Re_{\rm G}$ $Re_{\rm L}$ $R_{\rm W}$ $Sc_{\rm G}$ $Sh_{\rm G}$ T $T_{\rm G}$ $T_{\rm G}$ U U $w_{\rm G}$	mass transfer coefficient (m/s) thermal conductivity of liquid (J/s m K) height of the column (m) volumetric flow rate of gas (m ³ /s) rate of reaction (kmol/m ³ s) gas constant (J/kmol K) rate of gas absorption (kg/s) gas-phase Reynolds number, $(d - 2\delta)u_G\rho_G/\mu_G$ liquid-phase Reynolds number, $4\Gamma/\mu_L$ ratio of the interfacial area in the presence of waves to the plane interfacial area Schmidt number, $\mu_G/\rho_G D_G$ Sherwood number, $k_G a_c d/D_G$ liquid temperature (K) gas-phase temperature (K) inlet liquid temperature (K) temperature of cooling water (K) axial velocity of liquid film (m/s) velocity of gas film (m/s) overall heat transfer coefficient for cooling water (J/s m ² K) molar flow rate of gas per unit wetted perimeter (kmol/(m s))	
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Greek letters

α	thermal diffusivity (m ² /s)
β	function of liquid film Reynolds num

- β function of liquid film Reynolds number, defined in Eq. (16)
- Γ volumetric liquid flow rate (m³/s)
- δ liquid film thickness (m)
- μ liquid viscosity (kg/m s)
- ν kinematic viscosity of liquid (m²/s)
- ρ liquid density (kg/m³)
- τ shear stress (N/m²)

Subscripts

G	gas	phase
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- i interface
- in inlet
- L liquid phase
- out outlet

realistic fluid mechanics to model the liquid film flow. Several researchers [9-18] have illustrated the mass transfer studies, in particular, for the chemical absorption of CO₂ into aqueous solutions of amines like monoethanolamine (MEA), diethanolamine (DEA) and methyl-diethanol amine (MDEA) and its mixtures. Among them, the use of aqueous MEA solutions as absorbent takes more share in the industrial processes of CO₂ removal and research concerned have been reported [14–16]. Recently, sterically hindered amines such as 2-amine-2-methyl-1-propanol (AMP) have also found commercial application in gas treating industries.

The present work is to develop a mathematical model that can predict the non-isothermal absorption using observational knowledge of configurations and motion of the film. An empirical correlation for the dimensionless mass transfer coefficients, (Sh_G) in falling film reactor at low Reynolds numbers is determined based on the experimental investigations, which was used directly in the modeling equations. Experimental results were utilized in estimating gas-absorption performance in a continuous film contactor.

2. CO₂ absorption experiments

2.1. Apparatus and procedure

The schematic diagram of the experimental setup is shown in Fig. 1. The setup consists of three major sections: (1) the main part of the unit or the reactor section consisting of jacketed tubular falling liquid film column, (2) the liquid flow section consisting of the trough and peristaltic pump and (3) gas collection section consisting of gas sampler and a gas-chromatograph for identifying the gaseous components.

The reactor was made of glass (inner diameter 0.014 m, length 1 m) and cooling water was circulated through the jacket. The liquid was fed by peristaltic pump into the trough (holding capacity \sim 0.12 mL) of the liquid flow section from where it was made



Fig. 1. Experimental setup.

to flow downward wetting the walls of the reactor. Feed gas (a mixture of CO_2 and N_2) was introduced from the bottom of the reactor and flows upward in the main reaction section counter current to the liquid phase.

All the experiments were conducted at 298 K temperature and 1 atm pressure. CO_2 gas was diluted to the desired concentration with nitrogen before entering the reactor. The absorbent (30% aqueous MEA) selectively absorbs the CO_2 gas from the feed gas mixture and reacts simultaneously to form a stable carbamate in the reactor section. The gas samples were analysed using a gas chromatograph with Chromosorb 104 packed column in conjunction with a Model WinAcds 6.2 (Aimil Ltd.). The inlet and outlet gas-phase composition was determined using thermal conductivity detector with helium used as carrier gas (flow rate of 25 cm³/min). Oven, injector and detector temperatures were kept at 363 K, 383 K and 373 K respectively. Knowing the inlet and exit gas (CO_2) composition, the mass rate of absorption was calculated.

The properties of the absorbent i.e., 30 wt.% aqueous MEA solution, and of the CO₂-absorbent system are summarized in Table 1. The gas and liquid flow rates used were 1.67×10^{-5} to 5.0×10^{-5} m³/s and 1.04×10^{-7} to 4.72×10^{-7} m³/s respectively. The higher velocity of the MEA solution was determined so as to maximize the flow while the lower one was set close to the lower border of the stable film flow.

2.2. Results and discussion

For evaluating the effectiveness of CO_2 transfer, rate of absorption (mass based), R_A defined as

$$R_{\rm A} = Q_{\rm G}c_{\rm out} - Q_{\rm G}c_{\rm in} \tag{1}$$

was used, where c denotes the mass of CO₂ transferred from a unit volume of the gaseous mixture, and subscripts "in" and "out" indicate the gas mixture sampled before and after the liquid

Physical and chemical properties of CO₂-MEA system, temperature 298 K and a total pressure of 101.32 kPa

Absorbent	30 wt.% MEA solution
Density, $\rho_{\rm L}$ (kg/m ³)	1010
Viscosity, $\mu_{\rm L}$ (kg/m s)	2.41×10^{-3}
Thermal conductivity, k_{λ} (W/m K)	0.4837
Surface tension (N/m)	55.1×10^{-3}
Liquid diffusivity of CO_2 , D_A (m ² /s)	1.42×10^{-9}
MEA diffusivity $D_{\rm B}$ (m ² /s)	1.10×10^{-9}
Diffusivity of CO ₂ in gas, D_G (m ² /s)	1.67×10^{-5}
Density of gas mixture, $\rho_{\rm G}$ (kg/m ³)	1.248
Viscosity of gas mixture, $\mu_{\rm G}$ (kg/m s)	1.72×10^{-5}
Henry constant, H_0 (kmol/m ³ kPa)	0.316×10^{-3}
Heat of reaction (kJ/kmol)	65,000
Heat of solution (kJ/kmol)	19,500



Fig. 2. Effect of CO₂ concentration on rate of absorption, $u_{\rm G} = 0.3236$ m/s, $u_{\rm L} = 0.0412$ m/s, MEA concentration = 30 wt.%.

flowing down the test column. The effect of operating parameters on CO_2 absorption was studied by conducting series of experiments by varying CO_2 partial pressure, amine concentration and gas–liquid flow rates. It was observed that with increase in CO_2 partial pressure, the rate of absorption increases (Fig. 2). This is because; higher CO_2 mole fraction enhances the rate of interfacial transfer by lowering the gas side mass transfer resistance. The increase in gas velocity also exhibited similar behaviour on the rate of absorption (Fig. 3). This contributes to enhanced rate of mass transfer associated with the higher gas Reynolds number due to the interfacial turbulence caused by large ampli-



Fig. 3. Effect of gas velocity on rate of absorption for different CO₂ concentrations, $u_L = 0.0412 \text{ m/s}$, MEA concentration = 30 wt.%.



Fig. 4. Effect of liquid velocity on rate of absorption for different CO₂ concentrations, $u_G = 0.3467$ m/s, MEA concentration = 30 wt.%.

tude waves. The effect of changing liquid flow was studied and found that higher liquid flow rate presumably increases the rate of absorption (Fig. 4). This effect is surmised to occur due to the increase in film thickness, which leads to larger concentration gradient thereby increasing R_A . The rate of absorption was found to increase with the increase in MEA concentration (Fig. 5). Use of higher liquid composition results in more reaction due to more film thickness. Moreover, the higher viscosity may cause the liquid to flow down the reactor more slowly, yielding a longer residence time in the test column for a fixed liquid velocity.

2.3. Mass transfer correlation

A differential mass balance over the gas phase for the absorbed component results in the following equation for mass transfer coefficient ($k_{\rm G}$):

$$k_{\rm G} = \frac{Q_{\rm G}}{\pi (d - 2\delta) R_{\rm w} L} \ln\left(\frac{C_{\rm AGin}}{C_{\rm AGout}}\right)$$
(2)

where R_w is the ratio of the interfacial area in the presence of waves to the plane interfacial area. Its value is equal to 1 for plane liquid films and is >1 for wavy films of very high flow rates. Since the liquid film is not plane, a correction factor, a_c , is to be introduced and defined as [19],

$$a_{\rm c} = \left(\frac{d-2\delta}{d}\right) R_{\rm w} \tag{3}$$



Fig. 5. Effect of MEA composition on rate of absorption for $u_{\rm G} = 0.3467$ m/s, $u_{\rm L} = 0.0412$ m/s, CO₂ concentration = 30 mol%.



Fig. 6. Experimental gas-phase mass transfer coefficient data (symbols) compared with fitted correlation, Eq. (5) (solid line).

Eq. (2) is rewritten by the use of Eq. (3) and the following corresponding expression is obtained:

$$\frac{Q_{\rm G}}{\pi d} \ln\left(\frac{C_{\rm AGin}}{C_{\rm AGout}}\right) = k_{\rm G} a_{\rm c} L \tag{4}$$

All the uncertainities concerning the interfacial area are lumped into the final data and expressed as $k_G a_c$.

The modified gas-phase mass transfer coefficient, k_Ga_c , was calculated from Eq. (4) at different gas and liquid flow rates. The other terms of the equations were determined experimentally. Experimental data and the fitted correlation, given by Eq. (5), were compared in Fig. 6, in which $Sh_G/Sc_G^{0.5}$ is plotted against Re_G for five different values of Re_L . All these dimensionless numbers are defined in nomenclature. The correlation is based on 55 data points and predicts the experimental data with a mean deviation of 3.9%

$$Sh_{\rm G} = 0.0387 Re_{\rm G}^{0.66} Re_{\rm L}^{0.115} Sc_{\rm G}^{0.5}$$
⁽⁵⁾

The coefficients of Eq. (5) are estimated using non-linear leastsquare regression by fitting the expression to the experimental data. The correlation is valid for $Re_G \in [115; 350]$ and $Re_L \in [4; 32]$ at 298 K. The dependency of Re_L is probably due to changes in the interfacial area and increased turbulence of the fluid phases. It was not possible to find any suitable correlations in the literature for comparison with Eq. (5) because earlier investigations were conducted at higher Reynolds number.

3. Modeling of chemical gas-absorption

A numerical model has been developed for predicting the rate of absorption of any species initially mixed in a gas phase by a chemically reactive liquid flowing down a reactor wall. It has been modified according to the CO_2 -MEA system with CO_2 as gas species and MEA as liquid for better comparison and for validating with the experimental results described in the preceding section.

3.1. Basic assumptions

The basic assumptions considered for the CO_2 absorption by MEA solution in a falling film flow are listed below:

- 1. The physical properties of the liquid are held constant over the entire gas–liquid contact section irrespective of the special variation in the concentration of the liquid due to its absorption of CO₂.
- 2. The film thickness is small compared to the column diameter.
- 3. The liquid film is symmetric with respect to the reactor axis.
- 4. The CO₂ solubility in the liquid reactant and in the reaction products is in accordance with the Henry's law.
- 5. The liquid reactant is assumed to be non-volatile at working temperatures.

Assumption (1) is surmised to be reasonably accurate because the axial change in liquid composition in the gas–liquid contact section is expected to be insignificant. It should be noted that since the film thickness is very small compared to the column radius, and since the flow is symmetric in vertical annular flow, the flow is formulated as two-dimensional, and a Cartesian coordinate system is used instead of cylindrical coordinates, thus simplifying the model.

3.2. Formulation

3.2.1. CO₂-MEA reaction

The overall reaction occurring in the liquid phase may be expressed as

$$CO_2 + 2RNH_2 \rightarrow RNH_3^+ + RNHCOO^-$$
 (6)

where R indicates HCOH₂CH₂. This overall reaction is second order, i.e., first order with respect to CO₂ and MEA separately [20], and thus the reaction rate *r*, being defined as the molar rate of loss of CO₂ per unit volume, is expressed in terms of a reaction rate constant k and molar concentrations of CO₂ and MEA, C_A and C_B , as follows:

$$r = kC_{\rm A}C_{\rm B} \tag{7}$$

where k can be calculated, using the empirical correlation given by Hikita et al. [20].

3.2.2. Model equations

The modeling includes all the three transfer processes i.e., mass, momentum and heat to study the coupled effect of temperature and concentration on the rate of absorption. The developed equations include both ordinary differential equations (ODE's) and partial differential equations (PDE's) of non-linear nature. The flow model is described in Fig. 7.

The coupled partial differential equations representing the mass and heat balances for reaction

$$A(G) + bB(L) \rightarrow Product$$
 (8)

can be written as follows.

3.2.2.1. Liquid phase.

(i) Momentum balance



Fig. 7. Flow model of the film reactor.

The governing differential equation describing the momentum balance is given as:

$$\frac{\mathrm{d}\tau_{xz}}{\mathrm{d}x} = \rho g \tag{9}$$

Applying the following boundary conditions gives velocity distribution as given by Eq. (11), where

• Boundary conditions

At
$$x = 0$$
, interface, $\tau_{xz} = \tau_i = -\tau_G$,
At $x = \delta$, wall, $u_L = 0$ (10)

• Velocity distribution

$$u_{\rm L} = \frac{\rho_{\rm L}g}{2\mu_{\rm L}} \delta^2 \left[1 - \left(\frac{x}{\delta}\right)^2 \right] - \frac{\tau_{\rm G}\delta}{\mu_{\rm L}} \left[1 - \left(\frac{x}{\delta}\right) \right] \qquad (11)$$

Film thickness, δ is calculated from the volumetric rate of liquid obtained by the integration of the velocity distribution (Eq. (11)) and is given as

$$\Gamma = \frac{\rho g}{3\mu} \delta^3 - \frac{\tau_{\rm G} \delta^2}{2\mu} \tag{12}$$

where

$$\tau_{\rm G} = f \rho_{\rm G} u_{\rm G}^2 \tag{13}$$

The friction factor, f was evaluated using the relations proposed by Henstock and Hanratty [21], which accounts for the irregularities at the surface of the liquid layer and is given by

$$\frac{f}{2} = \begin{cases} \frac{8}{Re_{\rm G}} & Re_{\rm G} < 2000\\ \frac{Re_{\rm G}^{0.33}}{3050} & 2000 < Re_{\rm G} < 4000\\ \frac{0.04}{Re_{\rm G}^{0.25}} & Re_{\rm G} > 4000 \end{cases}$$
(14)

To account for the two-phase flow nature, the friction factor for $Re_G > 4000$ given by Eq. (14) should be multiplied by a term (1 + 1400*F*) where for the laminar liquid film,

$$F = \frac{\beta(Re_{\rm L})}{Re_{\rm G}^{0.9}} \frac{\nu_{\rm L}}{\nu_{\rm G}} \frac{\rho_{\rm L}}{\rho_{\rm G}} \left[1 - \exp\left(-\frac{\tau_{\rm G}}{\rho_{\rm L}g\delta}\right) \right]$$
(15)

in which

$$\beta = [(0.707 R e_{\rm L}^{1/2})^{2.5} + (0.0379 R e_{\rm L}^{0.9})^{2.5}]^{0.4}$$
(16)

- (ii) Mass balance
 - For component A:

$$u_{\rm L}\frac{\partial C_{\rm A}}{\partial z} = \frac{\partial}{\partial x} \left[D_{\rm A}\frac{\partial C_{\rm A}}{\partial x} \right] - kC_{\rm A}C_{\rm B}$$
(17)

• For component B:

$$u_{\rm L}\frac{\partial C_{\rm B}}{\partial z} = \frac{\partial}{\partial x} \left[D_{\rm B}\frac{\partial C_{\rm B}}{\partial x} \right] - kbC_{\rm A}C_{\rm B}$$
(18)

(iii) Heat balance

$$u_{\rm L}\frac{\partial T}{\partial z} = \frac{\partial}{\partial x} \left[\alpha \frac{\partial T}{\partial x} \right] + \left(\frac{\Delta H_{\rm R}}{\rho c_p} \right) k C_{\rm A} C_{\rm B}$$
(19)

• Boundary equations:

For $x = \delta$ at the wall

$$\frac{\partial C_A}{\partial x} = 0, \qquad \frac{\partial C_B}{\partial x} = 0,$$
$$-k_\lambda \frac{\partial T}{\partial x} = U(T_{x=0} - T_R) \tag{20}$$

For x = 0 at the interface

$$k_{\rm G}(C_{\rm AG} - C_{\rm A}H_{\rm o}) = -D_{\rm A}\frac{\partial C_{\rm A}}{\partial x}, \qquad \frac{\partial C_{\rm B}}{\partial x} = 0,$$
$$h_{\rm G}(T - T_{\rm G}) - k_{\lambda}\frac{\partial T}{\partial x} = (-\Delta H_{\rm s})\left[D_{\rm A}\frac{\partial C_{\rm A}}{\partial x}\right] \qquad (21)$$

At z = 0,

$$C_{\rm A} = 0, \qquad C_{\rm B} = C_{\rm B}^{\rm o}, \qquad T = T_{\rm o}$$
 (22)

- *3.2.2.2. Gas phase.*
- (i) Mass balance

$$\frac{\mathrm{d}w_{\mathrm{G}}C_{\mathrm{AG}}}{\mathrm{d}z} = k_{\mathrm{G}}(C_{\mathrm{AG}} - H_{\mathrm{o}}C_{\mathrm{A}}) \tag{23}$$

(ii) Heat balance

$$\frac{d(w_{\rm G}c_{\rm G}T_{\rm G})}{dz} = h_{\rm G}(T_{x=0} - T_{\rm G})$$
(24)

3.3. Numerical solution procedure

The mathematical relations were incorporated into an iterative solution procedure to elucidate the rate of CO_2 absorption changes with respect to the fall distance of the MEA solution. The algorithm for the numerical model is given in Appendix



Fig. 8. Comparison of predicted R_A with corresponding experimental data (effect of changing CO₂ concentration).



Fig. 9. Comparison of predicted R_A with corresponding experimental data (effect of changing gas flow rate).

A. The complexity of the model can be seen from the counter current flow direction of the two phases resulting into two iterative loops, whereas all the mathematical models reported in the past [1–8] are for co-current flow thus simplifying the numerical procedure. These coupled PDE's were solved using backward implicit finite difference numerical scheme. Implicit trapezoidal scheme was used to solve the gas-phase heat and mass transport equations. The tridiagonal matrix obtained from the discretization of highly coupled partial differential equation was solved using a subroutine wherein the $M \times M$ matrix was modified into $M \times 3$ matrix thereby reducing the computer storage space and processing speed [22].

By specifying the experimental conditions and physical properties of the MEA solution and of the CO₂/MEA binary system, $C_{AG}(z)$ was computed and subsequently R_A , the rate of absorption defined by Eq. (1) in which c_{in} and c_{out} should be read as $C_{AG,z=L}$ and $C_{AG,z=0}$ respectively. The results thus obtained are exemplified in Figs. 8–11 together with corresponding experimental results. The goodness of fit between



Fig. 10. Comparison of predicted R_A with corresponding experimental data (effect of changing liquid flow rate).



Fig. 11. Parity plot of experimental and predicted values.

predicted and experimental data indicates the practical utility of the chemical absorption model described above in predicting actual gas-absorption performance of a falling film reactor.

4. Conclusion

CO₂ absorption by MEA in a continuous film contactor has been experimentally analyzed and found better than other conventional processes. The proposed numerical scheme simulating the results based on momentum, mass and heat balance provides a mechanistic interpretation of the experimental results, and a means to predict the gas-absorption performance at arbitrary adjustments of operational parameters such as reactants (gas and liquid) concentration, flow rate of the absorbent, and flow rate of the gas mixture. The gas-phase mass transfer coefficient was also measured for laminar range of gas and liquid-phase Reynolds numbers. Reasonably good agreement between the model predictions and corresponding experimental results supports the general validity of the physical view underlying the model. The effect of gas and liquid temperature on the rate of absorption will be the next phase of this study.





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